



Universal Multiple Octet Coded Character Set  
International Organization for Standardization  
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**Title:** Additional Mathematical Symbols  
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The set of mathematical symbols proposed for addition to ISO/IEC 10646-1 and Unicode is based on an extensive search of existing mathematical literature. By its very nature, such a search can never be exhaustive, least of all for a notation that is a living and productive as mathematical notation. In order to have a workable proposal, the set was arbitrarily frozen at around the time it was first submitted to WG2.

All additional candidate characters for encoding that were found during the lengthy review phase for the original proposal were tracked separately, in order to confine the more tentative characters to a small manageable set. In the meantime, many, if not most of the characters in this secondary, but much smaller set have been confirmed.

An ad-hoc group consisting of the authors of this document, with input from Michael Everson, Ken Whistler and Murray Sargent have narrowed the candidate characters down to the list presented here and provided suggested names and annotations.

### **Format of this document**

While the format of this document follows that of a Unicode character names list, no code locations are suggested and many of the annotations are provided mainly for the readers and reviewers of this document; they are not intended to become part of the standard. A few already existing characters are shown for comparison purposes. These are clearly noted in the list of names; there is no intention to request duplicate encodings for them.

In some cases compatibility ‘mappings’ with novel tags can be found in the names list. These are indications of glyphic or semantic relations between characters, not as formal decompositions. In the final standard they would be replaced by simple cross-references.

	F52	F53	F54	F55	F56	F57	F58	F59	F5A	F5B	F5C	F5D	F5E	F5F
0		 F530		 F550	 F560	 F570	 F580	 F590	 F5A0					
1	 F521	 F531	 F541	 F551		 F571	 F581	 F591	 F5A1					
2		 F532	 F542	 F552	 F562	 F572	 F582	 F592	 F5A2					
3	 F523	 F533	 F543	 F553	 F563	 F573	 F583	 F593	 F5A3					
4		 F534	 F544	 F554	 F564	 F574	 F584	 F594	 F5A4					
5	 F525	 F535	 F545	 F555	 F565		 F585	 F595	 F5A5					
6	 F526	 F536	 F546	 F556	 F566	 F576	 F586	 F596	 F5A6					
7	 F527	 F537	 F547	 F557	 F567		 F587	 F597	 F5A7					
8	 F528	 F538	 F548	 F558	 F568	 F578	 F588		 F5A8					
9		 F539	 F549	 F559	 F569	 F579	 F589		 F5A9					
A	 F52A	 F53A	 F54A	 F55A	 F56A	 F57A	 F58A							
B		 F53B		 F55B	 F56B	 F57B	 F58B							
C	 F52C	 F53C			 F56C		 F58C							
D	 F52D	 F53D			 F56D		 F58D							
E	 F52E	 F53E		 F55E	 F56E		 F58E							
F	 F52F			 F55F	 F56F		 F58F							

- F521  $\Upsilon$  CROWN PRODUCT  
• weak candidate, marginal
- F522  $\text{\textcircled{R}}$  <reserved>
- F523  $\text{\textcircled{L}}$  LEFT AND RIGHT DOUBLE TURNSTILE
- F524  $\text{\textcircled{S}}$  <reserved>
- F525  $\text{\textcircled{F}}$  LEFT MULTIMAP  
= continuous Fourier transform  
→ 22B8  $\text{\textcircled{F}}$  multimap
- F526  $\text{\textcircled{D}}$  LONG RIGHT TACK  
= discrete Fourier transform
- F527  $\text{\textcircled{L}}$  LONG LEFT TACK
- F528  $\text{\textcircled{U}}$  UP TACK WITH CIRCLE ABOVE  
= radial component
- F529  $\text{\textcircled{Z}}$  <reserved>
- F52A  $\text{\textcircled{H}}$  ZONAL SPHERICAL FUNCTION  
• weak candidate
- F52B  $\text{\textcircled{G}}$  <reserved>
- F52C  $\text{\textcircled{E}}$  GLEICH STARK  
= tautological equivalent
- F52D  $\text{\textcircled{C}}$  COMBINING LEFTWARD ARROW OVERLAY
- F52E  $\text{\textcircled{W}}$  WHITE SQUARE WITH LEFTWARDS TICK  
= was always
- F52F  $\text{\textcircled{R}}$  WHITE SQUARE WITH RIGHTWARDS TICK  
= will always be
- F530  $\text{\textcircled{N}}$  WHITE CONCAVE-SIDED DIAMOND WITH LEFTWARDS TICK  
= was never
- F531  $\text{\textcircled{E}}$  WHITE CONCAVE-SIDED DIAMOND WITH RIGHTWARDS TICK  
= will never be
- F532  $\text{\textcircled{X}}$  WINDSCHIEF  
= skew  
• weak candidate
- F533  $\text{\textcircled{U}}$  UPWARDS QUADRUPLE ARROW
- F534  $\text{\textcircled{D}}$  DOWNWARDS QUADRUPLE ARROW

**Go markers**

- F535  $\text{\textcircled{O}}$  WHITE CIRCLE WITH DOT RIGHT
- F536  $\text{\textcircled{O}}$  WHITE CIRCLE WITH TWO DOTS
- F537  $\text{\textcircled{O}}$  BLACK CIRCLE WITH WHITE DOT RIGHT
- F538  $\text{\textcircled{O}}$  BLACK CIRCLE WITH WHITE TWO DOTS
- F539  $\text{\textcircled{O}}$  GRAY CIRCLE WITH GRAY DOT RIGHT  
• what is black should be gray in final font
- F53A  $\text{\textcircled{O}}$  GRAY CIRCLE WITH GRAY TWO DOTS  
• what is black should be gray in final font
- F53B  $\text{\textcircled{O}}$  GRAY FILLED CIRCLE WITH WHITE DOT RIGHT  
• what is black should be gray in final font

- F53C  $\text{\textcircled{O}}$  GRAY FILLED CIRCLE WITH WHITE TWO DOTS  
• what is black should be gray in final font

**Other Symbols**

- F53D  $+$  TINY
- F53E  $-$  MINY
- F53F  $\text{\textcircled{R}}$  <reserved>
- F540  $\text{\textcircled{S}}$  <reserved>
- F541  $\perp$  LARGE UP TACK  
 $\approx$  <large> 22A5  $\perp$  up tack
- F542  $\text{\textcircled{T}}$  LARGE DOWN TACK  
 $\approx$  <large> 22A4  $\text{\textcircled{T}}$  down tack
- F543  $($  LEFT BLACK TORTOISE SHELL BRACKET  
 $\approx$  <black> 3014  $[$  left tortoise shell bracket
- F544  $)$  RIGHT BLACK TORTOISE SHELL BRACKET  
 $\approx$  <black> 3015  $]$  right tortoise shell bracket
- F545  $\text{\textcircled{L}}$  LEFT WIGGLY FENCE
- F546  $\text{\textcircled{R}}$  RIGHT WIGGLY FENCE
- F547  $-$  BOLD MINUS SIGN  
→ 2212  $-$  minus sign
- F548  $\text{\textcircled{X}}$  LEFT OUTER JOIN
- F549  $\text{\textcircled{X}}$  RIGHT OUTER JOIN
- F54A  $\text{\textcircled{X}}$  FULL OUTER JOIN
- F54B  $\text{\textcircled{S}}$  <reserved>
- F54C  $\text{\textcircled{S}}$  <reserved>
- F54D  $\text{\textcircled{S}}$  <reserved>
- F54E  $\text{\textcircled{S}}$  <reserved>
- F54F  $\text{\textcircled{S}}$  <reserved>
- F550  $\%$  COMMERCIAL MINUS SIGN
- F551  $\text{\textcircled{L}}$  COMMERCIAL MINUS SIGN  
• glyph variant of F550  $\%$  - candidate for VS1?
- F552  $\text{\textcircled{R}}$  RIGHT ARROW WITH SMALL CIRCLE
- F553  $\text{\textcircled{R}}$  RIGHT ARROW WITH CIRCLED PLUS
- F554  $\text{\textcircled{R}}$  IRREFLEXIVE PARTIAL ORDER  
• weak candidate
- F555  $\text{\textcircled{R}}$  X-F555  
• weak candidate - no suggested name
- F556  $\text{\textcircled{R}}$  PARTIAL ORDER  
• weak candidate
- F557  $\text{\textcircled{R}}$  DIJKSTRA CHOICE
- F558  $\text{\textcircled{R}}$  N-ARY DIJKSTRA CHOICE
- F559  $\text{\textcircled{R}}$  AND WITH DOT
- F55A  $\text{\textcircled{R}}$  LARGE TRIPLE VERTICAL BAR OPERATOR  
often n-ary  
→ 2AF4  $\text{\textcircled{R}}$  triple vertical bar binary relation  
→ 2980  $\text{\textcircled{R}}$  triple vertical bar delimiter
- F55B  $\text{\textcircled{R}}$  TRIPLE SOLIDUS BINARY RELATION  
= triple slash binary relation  
→ 2AF4  $\text{\textcircled{R}}$  triple vertical bar binary relation
- F55C  $\text{\textcircled{S}}$  <reserved>
- F55D  $\text{\textcircled{S}}$  <reserved>

- F55E ◊ LOZENGE DIVIDED BY HORIZONTAL RULE
- F55F † LEFT AND RIGHT TACK
- F560 ◻ SQUARED DOT  
→ 29C7 ◻ squared small circle
- F561 ◻ <reserved>
- F562 < LEFT POINTING CURVED ANGLE BRACKET  
→ 2329 < left pointing angle bracket
- F563 > RIGHT POINTING CURVED ANGLE BRACKET  
→ 232A > right pointing angle bracket
- F564 ∪ ELEMENT OF OPENING UPWARDS  
→ 2AD9 ∩ element of opening downwards
- F565 ↙ LOWER RIGHT CORNER WITH DOT  
= pullback
- F566 ↖ UPPER LEFT CORNER WITH DOT  
= pushout
- F567 ≡ LEFT DOUBLE WIGGLY FENCE
- F568 ≡ RIGHT DOUBLE WIGGLY FENCE
- F569 ◻ INVISIBLE COMMA  
= invisible separator

### Diamonds

*Diamonds are needed in several sizes, the sizes here are from an existing and widely available set of fonts*

- F56A · BLACK TINY DIAMOND
- F56B · BLACK VERY SMALL DIAMOND
- F56C · BLACK SMALL DIAMOND
- F56D ◆ BLACK MEDIUM DIAMOND
- F56E ◆ BLACK DIAMOND  
• not a candidate - shown for comparison only  
≡ 25C6 ◆ black diamond
- F56F ◆ BLACK LARGE DIAMOND

### On-line

- F570 . MULTIPLICATION ON-LINE  
= often omitted  
→ F571 . on-line dot
- F571 . ON-LINE DOT  
= paired, used as fence  
→ F570 . multiplication on-line

### Relations

- F572 ≪ STACKED VERY MUCH LESS-THAN  
≈ <stacked> 22D8 ≪≪ very much less-than
- F573 ≫ STACKED VERY MUCH GREATER-THAN  
≈ <stacked> 22D9 ≫≫ very much greater-than
- F574 ≧ VARIANT LESS-THAN OVER EQUAL TO  
≈ <variant> 2266 ≧ less-than over equal to
- F575 ◻ <reserved>

- F576 ≧ VARIANT GREATER-THAN OVER EQUAL TO  
≈ <variant> 2267 ≧ greater-than over equal to
- F577 ◻ <reserved>
- F578 ⌚ CLOCKWISE
- F579 ⚙ ANTI CLOCKWISE
- F57A ≐ EQUALS WITH ASTERISK
- F57B ⌞ COMBINING WIDE BRIDGE ABOVE  
this character extends the full width of the base character  
→ 0346 ⌞ combining bridge above
- F57C ◻ <reserved>
- F57D ◻ <reserved>
- F57E ◻ <reserved>
- F57F ◻ <reserved>
- F580 // DOUBLE SLASH OPERATOR  
= tangential to

### Dice

- F581 ◻ DIE FACE-1
- F582 ◻ DIE FACE-2
- F583 ◻ DIE FACE-3
- F584 ◻ DIE FACE-4
- F585 ◻ DIE FACE-5
- F586 ◻ DIE FACE-6

### Lozenges

*Lozenges are needed in several sizes, the sizes here are from an existing and widely available set of fonts*

- F587 · BLACK TINY LOZENGE
- F588 · BLACK VERY SMALL LOZENGE
- F589 · BLACK SMALL LOZENGE
- F58A ◆ BLACK MEDIUM LOZENGE
- F58B ◆ FILLED LOZENGE  
• this is not a candidate - shown for comparison  
≡ 29EB ◆ filled lozenge
- F58C ◆ BLACK LARGE LOZENGE
- F58D ◊ DIAMOND OPERATOR  
• this is not a candidate - shown for comparison  
misnomer: this is a lozenge shape, not a diamond  
≡ 22C4 ◊ diamond operator
- F58E ◊ LOZENGE  
• this is not a candidate - shown for comparison  
≡ 25CA ◊ lozenge
- F58F ◊ LARGE LOZENGE
- F590 ◆ LARGE LOZENGE CONTAINING SMALL FILLED LOZENGE

## White Diamonds

*White diamonds are needed in at least two sizes, the sizes here are derived from the black diamonds. Widely available fonts have the large diamond only, Unicode 3.0 has the 'normal' size, and mathematical publications need at least one size smaller than the current size*

- F591 ◦ WHITE TINY DIAMOND
- F592 ◊ WHITE VERY SMALL DIAMOND
- F593 ◊ WHITE SMALL DIAMOND
- F594 ◊ WHITE MEDIUM DIAMOND
- F595 ◊ WHITE DIAMOND
  - this is not a candidate - shown for comparison
  - ≡ 25C7 ◊ white diamond
- F596 ◊ WHITE LARGE DIAMOND
- F597 ◈ WHITE LARGE DIAMOND CONTAINING BLACK SMALL DIAMOND
  - widely available fonts contain this symbol with two or three variations of the size of the inner diamond

## Long Arrows

*These have been proposed as variations or characters*

- F5A0 ← LONG LEFTWARDS ARROW
- F5A1 → LONG RIGHTWARDS ARROW
- F5A2 ↔ LONG LEFT RIGHT ARROW
- F5A3 ⇐ LONG LEFTWARDS DOUBLE ARROW
- F5A4 ⇒ LONG RIGHTWARDS DOUBLE ARROW
- F5A5 ⇔ LONG LEFT RIGHT DOUBLE ARROW
- F5A6 ←| LONG LEFTWARDS ARROW FROM BAR
  - = maps from
- F5A7 →| LONG RIGHTWARDS ARROW FROM BAR
  - = maps to
- F5A8 ⇐| LONG LEFTWARDS DOUBLE ARROW FROM BAR
- F5A9 ⇒| LONG RIGHTWARDS DOUBLE ARROW FROM BAR