Title: Towards an Encoding for Coptic Numbers in the UCS
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Status: Liaison Contribution
Action: For consideration by UTC
Date: 2010-04-10

## 1 Introduction

A set of characters used for representing numbers in Coptic was described by the present author in L2/09163R ("Proposal to Encode Coptic Numerals in ISO/IEC 10646"). Several changes to the original document have been made, including change of name of the script block from "Coptic Numerals" to "Coptic Numbers"; development of a draft font; addition of a code chart and names list; and allocation of the block in the Supplementary Multilingual Plane (SMP).

There are a few concerns regarding the character repertoire and the name for the script block. These issues are discussed in Section 6. Advice is sought from the Unicode Technical Committee and additional Copticists regarding these issues.

## 2 Background

The proposed characters are elements of a numeric notation system used in some Coptic manuscripts, which differ from the standard representation of numbers using letters of the alphabet. A comparison of the two systems is given in Table 1. The numbers are reputed to be 'cursive' forms of Coptic letters. In Grammaire Copte (1956), Alexis Mallon shows a possible derivation of the numbers from letters of the Coptic alphabet; he calls them 'cursive Coptic numbers' ("chiffres coptes cursifs"). It is believed that these numbers were used primarily in Coptic-Arabic manuscripts, such as that shown in Figure 2. They appear in Coptic manuscript fragments in the collection of the AHRC Rylands Cairo Genizah Project at the University of Manchester (Figure 3).

The Coptic Numbers were not included by Michael Everson in N2636 "Revised proposal to add the Coptic alphabet to the BMP of the UCS". The proposed Coptic Numbers appear in Figure 14 of N2636, an excerpt of which is given here in Figure 6. In the caption for the figure, Everson writes that "further study may indicate that some of the additional characters and symbols shown here should also be added to the Standard". Indeed, additional research has shown that the 'Signes de numération' illustrated in the figure were also described by Antoine P. Pihan in Exposé des signes de numération (see Figure 4). An encoding for the Coptic Numbers will enhance the Coptic repertoire by offering a means for representing characters used in Coptic-Arabic manuscripts.

## 3 Characters Proposed

The proposed code chart and names list are shown in Figure 1. Digits 1-9 are named Digit; all others are named number for consistency within the Universal Character Set.

## 4 The Notation System

Structure Coptic Numbers represent units of a positional decimal system. The system is additive, that is, the value of a number is the sum of the values of the numbers that constitute it. There is no character for zero; it is inherently represented in the distinct number for each decimal orders. The number are written left-to-right. The system has unique characters for representing decimal orders of the primary, tens, and hundreds units. The thousands are represented by writing a slash-mark beneath the numbers.

Orthography The thousands are represented by writing the primary number and thousands mark: $\boldsymbol{\varepsilon}$ five $+\underline{q}$ Thousands mark $=\boldsymbol{\varepsilon} 5,000$. The ten thousands are written using the tens number and the THOUSANDS MARK: $\boldsymbol{\nu}$ FIFTY + , THOUSANDS MARK $=\boldsymbol{\nu}, 50,000$. The hundred thousands are written with the numbers for the hundreds and the THOUSANDS MARK: $\boldsymbol{\mathcal { L }}$ FIVE HUNDRED $+\boldsymbol{q}$ THOUSANDS MARK $=\boldsymbol{\not} \boldsymbol{\sim} 500,000$.

Decimal orders larger than hundred thousand may be represented by stacking the thousands mark. This practice mirrors the principle of writing numbers using letters of the Coptic alphabet, where the overline $\bar{\circ}$ u+0305 Combining overline is doubled to indicate the orders of the thousands, eg. $\overline{\bar{\sigma}}$.

Composite numbers are produced using the primary numbers and the numbers of larger decimal orders. The larger numeral is written first, then the primary numeral: $\boldsymbol{\iota} \boldsymbol{\varepsilon} 25$ (TWENTY + FIVE); $\boldsymbol{\tau} \boldsymbol{\varepsilon} 205$ (TWO HUNDRED + FIVE); $\boldsymbol{\sigma} \boldsymbol{\nu} 250$ (TWO HUNDRED + FIFTY).

Numbers are marked using the COPTIC nUMBER MARK. The length of the number mark extends over the entire sequence of numbers: $\overline{\boldsymbol{L \varepsilon}} 15 ; \widetilde{\mathcal{L} \nu} 550 ; \overline{\boldsymbol{\varepsilon}_{\boldsymbol{\Psi}} \varepsilon} 5,505$.

## 5 Implementation

Allocation Coptic Numbers are allocated at the range U+102E0..U+102FF in the Supplementary Multilingual Plane (SMP).

Character Properties The proposed characters have the following properties:

```
102E0 COPTIC THOUSANDS MARK;Mn;0;NSM;;;;1000;N;;;;;
102E1 COPTIC DIGIT ONE;NO;0;L;;;;1;N;;;;;
102E2 COPTIC DIGIT TWO;NO;0;L;;;;2;N;;;;;
102E3 COPTIC DIGIT THREE;NO;O;L;;;;3;N;;;;;
102E4 COPTIC DIGIT FOUR;No;0;L;;;;4;N;;;;;
102E5 COPTIC DIGIT FIVE;No;0;L;;;;5;N;;;;;
102E6 COPTIC DIGIT SIX;NO;0;L;;;;6;N;;;;;;
102E7 COPTIC DIGIT SEVEN;NO;0;L;;;;7;N;;;;;
102E8 COPTIC DIGIT EIGHT;NO;O;L;;;;8;N;;;;;
102E9 COPTIC DIGIT NINE;No;0;L;;;;9;N;;;;;
102EA COPTIC NUMBER TEN;NO;0;L;;;;10;N;;;;;
102EB COPTIC NUMBER TWENTY;NO;0;L;;;;20;N;;;;;
102EC COPTIC NUMBER THIRTY;No;0;L;;;;30;N;;;;;
102ED COPTIC NUMBER FORTY;No;0;L;;;;40;N;;;;;
102EE COPTIC NUMBER FIFTY;NO;0;L;;;;50;N;;;;;
102EF COPTIC NUMBER SIXTY;NO;0;L;;;;60;N;;;;;
102FO COPTIC NUMBER SEVENTY;NO;0;L;;;;70;N;;;;;
102F1 COPTIC NUMBER EIGHTY;No;0;L;;;;80;N;;;;;
102F2 COPTIC NUMBER NINETY;NO;0;L;;;;90;N;;;;;
102F3 COPTIC NUMBER ONE HUNDRED;NO;0;L;;;;100;N;;;;;
102F4 COPTIC NUMBER TWO HUNDRED;NO;0;L;;;;200;N;;;;;
102F5 COPTIC NUMBER THREE HUNDRED;NO;0;L;;;;300;N;;;;;
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102F6 COPTIC NUMBER FOUR HUNDRED;No;0;L;;;;400;N;;;;;
102F7 COPTIC NUMBER FIVE HUNDRED;No;0;L;;;;500;N;;;;;
102F8 COPTIC NUMBER SIX HUNDRED;NO;0;L;;;;600;N;;;;;
102F9 COPTIC NUMBER SEVEN HUNDRED;NO;0;L;;;;700;N;;;;;;
102FA COPTIC NUMBER EIGHT HUNDRED;NO;0;L;;;;800;N;;;;;
102FB COPTIC NUMBER NINE HUNDRED;No;0;L;;;;900;N;;;;;
102FC COPTIC NUMBER MARK;SO;0;L;;;;;N;;;;;
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## 6 Issues

1. Name Based upon advice from the UTC, the name for the block was changed from 'Coptic Numerals' to 'Coptic Numbers'. Terry Wilfong, an Egyptologist, expressed concern with the name. He indicated that the numbers are a late innovation, not standard Coptic usage, and are used only in CopticArabic manuscripts. He suggested that the block be renamed in order to indicate the non-standard usage of the numbers. Would it be appropriate to rename the block as 'Coptic Arabic Numbers'?
2. Character Repertoire Michael Everson recommended against the encoding of coptic number mark, stating that Copticists would prefer to use $\mathbf{~}+0305$ Combining overline, as is the standard convention for writing numbers. Everson's recommendation is acceptable. However, does the UTC see any reason to include COPTIC NUMBER MARK?
3. Suitability for Encoding It is likely that the numbers are variations on the standard cursive forms of Coptic letters. However, the fact that they are depicted uniquely in Figure 4 and Figure 6 suggests that they were considered sufficiently distinct from the original alphabetic sources. Is it possible to unify these characters with existing Coptic letters or is an independent encoding justified?

## 7 References

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## 8 Acknowledgments

I would like to thank Traianos Gagos and Terry Wilfong, both of the University of Michigan, for sharing their comments on L2/09-163R.

This project was made possible in part by a grant from the United States National Endowment for the Humanities, which funded the Universal Scripts Project (part of the Script Encoding Initiative at the University of California, Berkeley). Any views, findings, conclusions or recommendations expressed in this publication do not necessarily reflect those of the National Endowment of the Humanities.


Figure 1: Proposed code chart and nameslist for Coptic Numbers


Table 1: Numbers written using Coptic Numbers (top) and the alphabetic system (bottom).


Fig. C. 6 Coptic numerals in a copy from ca. 1800 of a set of astronomical tables by the early-13thcentury Coptic scholar Ibn 'Assal. This notation has separate, unrelated symbols for the units, tens and hundreds, etc., and for simple fractions. (From MS Cairo DM 910,1, fol. 81v, courtesy of the Egyptian National Library.)

Figure 2: Excerpt of a manuscript showing the use of Coptic Numbers with the Arabic script (from King 2001: Appendix C, p. 299).

Figure 3: Coptic numbers in a manuscript fragment from the Rylands Genizah collection (from AHRC Rylands Cairo Genizah Project: fragment B 6548-1).


Figure 4: Table showing the forms of Coptic Numbers (from Pihan 1860: 213). Compare the Coptic Numbers to the alphabetic system system shown in Figure 7.


Figure 5: Table showing composite numbers written with Coptic Numbers (from Pihan 1860: 214).

## COPTE MEMPHITIQUE.

lettres alphabétiques.
majuscules.

minuscules.


SIGNES DE Numération.

$$
\begin{aligned}
& \dot{\omega} \mathscr{y} \geqslant \underline{\omega} \geqslant \underline{\varepsilon}, \underline{b} \underline{\theta}
\end{aligned}
$$

lettres nggentúes, higature et signes divers.
ì $\dot{\mathbf{E}}$ i is ir ì cir $\overrightarrow{\sigma \mathrm{C}} \mathrm{J}, \quad$,

Figure 6: Coptic Numbers for the primary, tens, hundreds, and thousands shown in a specimen of Coptic type under the heading 'Signes de numération'. Two length variants of the COPTIC NUMBER MARK are shown under the heading 'Lettres accentuées...' (reproduced from Everson 2003: Figure 14).


Figure 7: The representation of numbers in Coptic using letters of the alphabet and horizontal overlines (reproduced from Everson 2003: Figure 12).

| Chiffues coptes cursifs． |  |
| :---: | :---: |
| 1 a＞）${ }^{\text {a }}$ | 70 O\％ 0 \％ 8 |
| $2 \bar{B} \omega \omega$ | 80 in $\sigma$ 人 $\sigma$ |
| 3 ¢ $\quad$ ¢ $\quad$ r |  |
| $4 \overline{\text { à }}$ ¢ $) ~ 9$ | 100 P 222 |
| $5 \bar{\varepsilon}$ ¢ $\mathcal{L}$ | $200 \bar{C} \sim$ |
| ${ }^{6} \Sigma \varepsilon \varepsilon \varepsilon$ | 300 i $\tau \tau \mathcal{Z}$ |
| 子うろ333 | $400 \stackrel{\rightharpoonup}{\mathrm{~V}} \mathrm{C}$ |
| 8 －b b b | $500 \dot{\phi} \varphi$ |
| $9 \dot{\theta} \theta \theta \theta \theta$ | $600 \bar{\chi}$ ¢ |
| 10 i 」 J L L | $700 \%$ \％$\quad$ \％ |
| 20 k Le $\mathrm{L}_{4}$ | $800 \bar{\omega} \dot{\omega}$ |
| 30 a 5 J J | 900 ¢ 呆 そ V |
| 40 i $\psi \mathcal{L} \omega$ | 1000 匈 $\cong$ ） |
| 50 －$\delta \mu \mu$ | 2000 言 8 |
| $60 \xi d \mathrm{~d} \delta 0$ | 3000 F 「 |

Figure 8：Table showing the Coptic numbers（from Mallon 1956：234）．

